

Polynomial Review - Show all work on a separate sheet! Date _____ Period _____

Classify each by Degree and Number of terms, and then describe the end behavior of each function.

1) $f(x) = -x^2 - 2x - 3$

2) $f(x) = x^4 - 2x^2$

3) $f(x) = x^5 - 4x^3 + 2x - 2$

4) $f(x) = -x^4 + x^3 + 3x^2 - 4$

Factor each.

5) $f(x) = x^3 + 4x^2 - 3x - 12$

6) $f(x) = x^6 + 2x^4 - 16x^2 - 32$

7) $f(x) = x^4 - x^2 - 12$

8) $f(x) = x^4 - 13x^2 + 36$

9) $f(x) = x^3 + 125$

10) $f(x) = 3x^3 - 192$

Factor each and find all zeros.

11) $f(x) = 3x^3 + 8x^2 + 4x$

12) $f(x) = 2x^3 - x^2 - 6x$

13) $f(x) = 3x^3 + 4x^2 + 15x + 20$

14) $f(x) = 2x^3 + x^2 + 10x + 5$

15) $f(x) = 5x^3 - 25x^2 + 4x - 20$

16) $f(x) = 4x^3 - 20x^2 - 3x + 15$

17) $f(x) = x^3 + 27$

18) $f(x) = x^3 - 125$

Divide.

19) $(4m^3 + 28m^2 + 34m + 60) \div (m + 6)$

20) $(2n^3 - 20n^2 + 51n - 63) \div (n - 7)$

21) $(2n^4 - 19n^3 - n^2 + 9n) \div (2n - 1)$

22) $(4x^4 + 5x^3 + 19x^2 - 82x + 21) \div (4x - 7)$

Find all zeros. One zero has been given.

23) $f(x) = x^4 - 10x^3 + 32x^2 - 32x$; 2

24) $f(x) = x^4 + x^3 - 4x^2 + 6x$; -3

25) $f(x) = x^4 - 4x^3 + 9x^2 - 10x$; 2

26) $f(x) = x^4 - 5x^2 + 4$; 2

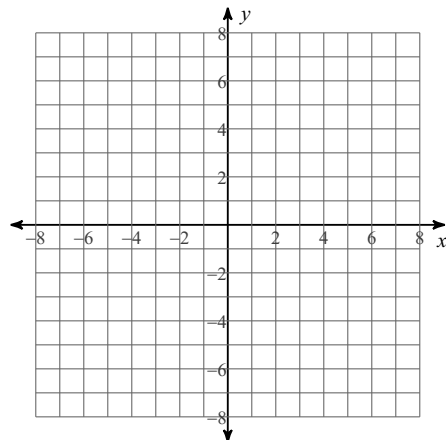
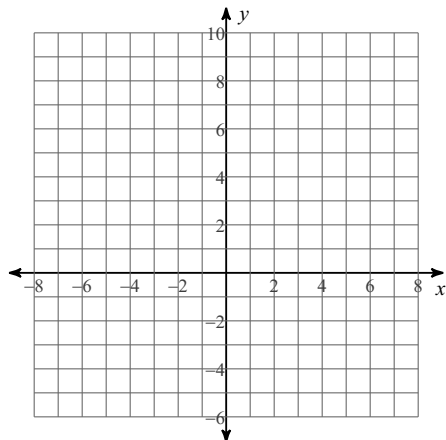
27) $f(x) = x^4 - x^3 - 34x^2 - 20x; -5$

28) $f(x) = x^4 - 24x^2 - 40x; -2$

Sketch the graph of each polynomial. Consider y-intercept, x-intercepts (and multiplicity), and end behavior.

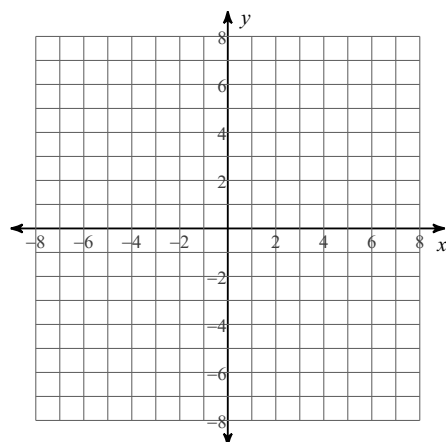
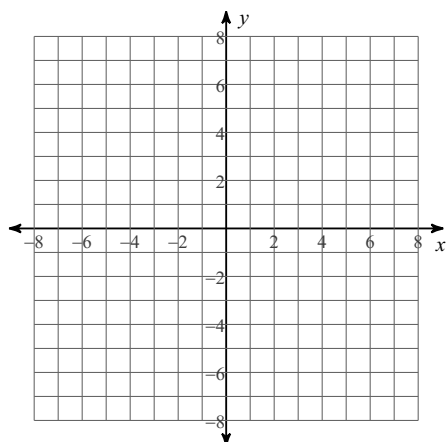
29) $y = (x + 1)^2(x - 3)(x - 2)$

30) $y = (x + 1)^2(x - 2)(x - 1)^2$



31) $y = x^3 - 3x^2 - x + 3$

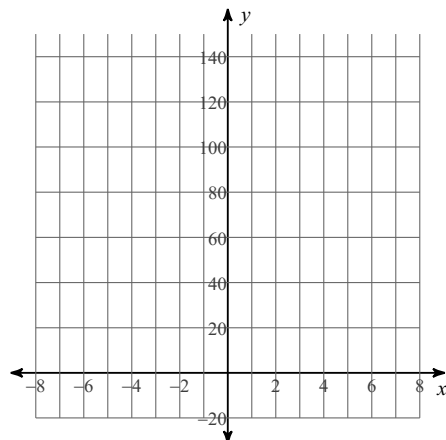
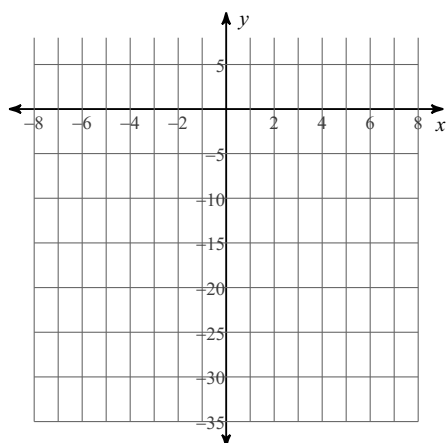
32) $y = -2x^4 - 8x^3 - 8x^2$



33) $y = x^3 + 3x^2 - 10x - 24$

Hint: One of the roots is -4

34) $y = -x^3 - 5x^2 + 25x + 125$



Answers to Polynomial Review - Show all work on a separate sheet!

1) Quadratic Trinomial

Falls to the left. Falls to the right

3) Fifth Degree Polynomial

Falls to the left. Rises to the right

5) $f(x) = (x + 4)(x^2 - 3)$

7) $f(x) = (x^2 + 3)(x - 2)(x + 2)$

9) $f(x) = (x + 5)(x^2 - 5x + 25)$

11) Factors to: $f(x) = x(3x + 2)(x + 2)$

Zeros: $\left\{0, -\frac{2}{3}, -2\right\}$

13) Factors to: $f(x) = (3x + 4)(x^2 + 5)$

Zeros: $\left\{-\frac{4}{3}, i\sqrt{5}, -i\sqrt{5}\right\}$

15) Factors to: $f(x) = (x - 5)(5x^2 + 4)$

Zeros: $\left\{5, \frac{2i\sqrt{5}}{5}, -\frac{2i\sqrt{5}}{5}\right\}$

17) Factors to: $f(x) = (x + 3)(x^2 - 3x + 9)$

Zeros: $\left\{-3, \frac{3 + 3i\sqrt{3}}{2}, \frac{3 - 3i\sqrt{3}}{2}\right\}$

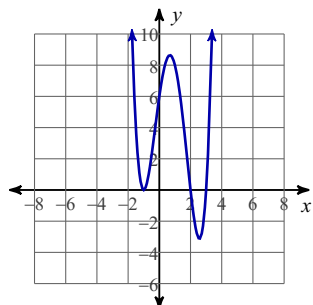
19) $4m^2 + 4m + 10$

20) $2n^2 - 6n + 9$

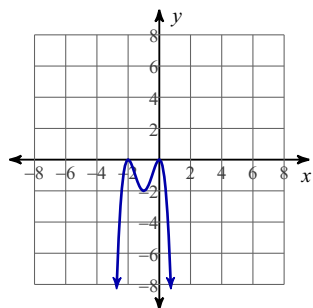
22) $x^3 + 3x^2 + 10x - 3$

26) $\{-2, 1, -1, 2\}$

29)



32)



2) Fourth Degree (Quartic) Binomial

Rises to the left. Rises to the right

4) Fourth Degree Polynomial

Falls to the left. Falls to the right

6) $f(x) = (x^2 + 2)(x - 2)(x + 2)(x^2 + 4)$

8) $f(x) = (x + 2)(x - 2)(x + 3)(x - 3)$

10) $f(x) = 3(x - 4)(x^2 + 4x + 16)$

12) Factors to: $f(x) = x(2x + 3)(x - 2)$

Zeros: $\left\{0, -\frac{3}{2}, 2\right\}$

14) Factors to: $f(x) = (2x + 1)(x^2 + 5)$

Zeros: $\left\{-\frac{1}{2}, i\sqrt{5}, -i\sqrt{5}\right\}$

16) Factors to: $f(x) = (x - 5)(4x^2 - 3)$

Zeros: $\left\{5, \frac{\sqrt{3}}{2}, -\frac{\sqrt{3}}{2}\right\}$

18) Factors to: $f(x) = (x - 5)(x^2 + 5x + 25)$

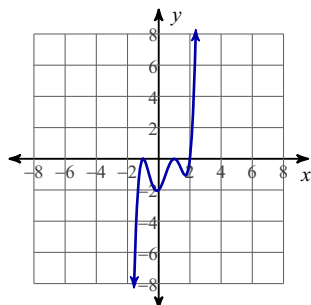
Zeros: $\left\{5, \frac{-5 + 5i\sqrt{3}}{2}, \frac{-5 - 5i\sqrt{3}}{2}\right\}$

21) $n^3 - 9n^2 - 5n + 2 + \frac{2}{2n - 1}$

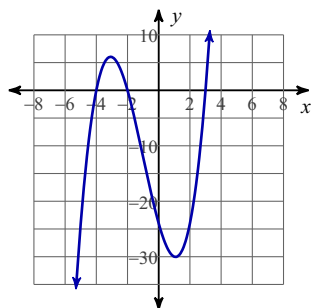
23) $\{0, 4 \text{ mult. } 2, 2\}$

27) $\{0, 3 + \sqrt{13}, 3 - \sqrt{13}, -5\}$

30)



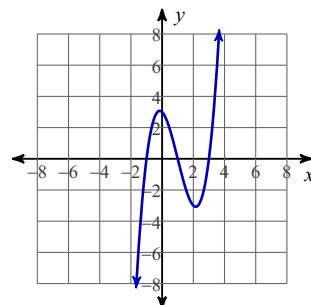
33)



24) $\{0, 1 + i, 1 - i, -3\}$

28) $\{0, 1 + \sqrt{21}, 1 - \sqrt{21}, -2\}$

31)



34)

